# **Special Feature: Materials Analysis**

#### Review

# A Powerful Tool to Characterize Lithium Insertion Materials for Advanced Lithium-ion Batteries: Macro- and Microscopic Magnetism Studied by Magnetic Susceptibility ( $\chi$ ) and Muon-spin Rotation/Relaxation ( $\mu$ SR) Measurements

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> **ABSTRACT**|| The macroscopic magnetism of lithium insertion materials for lithium-ion batteries is investigated using magnetic susceptibility ( $\chi$ ) measurements to obtain an insight into the interrelationship between the electrochemical, structural, and magnetic properties. A new technique of muon-spin rotation/relaxation ( $\mu$ SR) measurements is also introduced to determine the microscopic magnetism of lithium insertion materials. Here we report results on two structural types; the layered structure of LiCo<sub>1-x</sub>Ni<sub>x</sub>O<sub>2</sub> and the spinel-framework structure of Li[ $M_x$ Mn<sub>2-x</sub>]O<sub>4</sub> with M = Li, Mg, and Ni.

#### KEYWORDS

 Lithium-ion Battery, Lithium Insertion Material, Electric Vehicle, Magnetic Susceptibility (χ), Muon-spin Rotation/Relaxation (μSR), Layered Structure, Spinel-framework Structure

#### 1. Introduction

Over the past one hundred years, the internalcombustion engine system has been used as a power supply for vehicles. However, recent issues such as global warming, environmental pollution, and consumption of fossil fuel have prompted the production of more efficient and clean vehicles. One of the ultimate solutions is the electric vehicle (EV), which is powered by an electric motor with a rechargeable battery, because the EV needs no fuel, and exhausts no harmful gases such as nitrogen oxides  $(NO_x)$  and sulfur oxides  $(SO_x)$ . Furthermore, battery charging during the night time enables load balancing of the electrical power supply. There is no doubt that the performance of the rechargeable batteries used determines the performance of EV. Compared with rechargeable batteries such as lead-acid and nickelmetal hydride (Ni-MH) batteries, lithium-ion batteries (LIB) have attracted significant interest from battery researchers and electrochemists due to their highenergy density and wide variety of positive/negative electrode materials.<sup>(1)</sup> Figure 1 shows a schematic illustration of the operation principle of the LIB, which consists of two insertion electrode materials and a nonaqueous electrolyte. Lithium ions move back and forth between the positive and negative electrode materials during charge and discharge reactions. Electrons are simultaneously extracted from one electrode and injected into the other, storing and releasing electrical



**Fig. 1** Schematic illustration of the LIB operation principle. When the battery is charged, lithium ions in the positive electrode move to the negative electrode through the electrolyte. During discharge, lithium ions in the negative electrode return to the positive electrode, and discharge current flows. Thus, the LIB is charged and discharged only through the movement of lithium ions.

energy. Surprisingly, the framework structure of the lithium insertion material is maintained during the overall reaction. This reaction is referred to as *topotactic*, where *topo* and *tactic* mean 'place' and 'spatial arrangement', respectively, and this is a reason why LIBs can be used for more than one thousand cycles.

The commercial LIB is based on the report by Goodenough and co-workers; lithium cobalt oxide LiCoO<sub>2</sub>, having a layered structure with a space group of  $R\bar{3}m$  (see Fig. 2(a)), shows an operation voltage around 4 V vs. Li<sup>+</sup>/Li.<sup>(2)</sup> In 1991, Sony Corporation released a 750 mAh class LIB by selecting LiCoO<sub>2</sub> and petroleum coke as battery materials.<sup>(3)</sup> The rechargeable capacity of LiCoO<sub>2</sub> is limited to ca. 140  $mAh \cdot g^{-1}$  due to its structural instability;<sup>(4,5)</sup> therefore, possible alternatives to  $LiCoO_2$ , such as  $LiNiO_2$ ,<sup>(6-8)</sup>  $LiCo_{1-x}Ni_xO_2$ ,<sup>(9,10)</sup> $Li[Li_xMn_{2-x}]O_4$ ,<sup>(11-13)</sup> $Li[Ni_{1/2}Mn_{3/2}]O_4$ ,<sup>(14-16)</sup> and LiFePO<sub>4</sub>,<sup>(17,18)</sup> have been investigated over the past decades. However, the current LIB positive electrode materials consist mainly of the following 10 elements; Li, C, O, Al, P, Co, Mn, Fe, Co, and Ni, because of their high energy density, low toxicity, and inexpensive material cost. Thus, in order to find advanced lithium insertion materials by combination of these limited elements, we must understand the correlation between the fundamental physical (e.g. magnetic, electronic, and mechanical) properties and electrochemical properties of the materials currently used.

Among the many methods to characterize lithium insertion materials, magnetic susceptibility ( $\chi$ ) measurement is a powerful tool to investigate the local



Fig. 2 Crystal structures of (a)  $\text{Li}MO_2$  and (b)  $\text{Li}M_2O_4$ lithium insertion materials, where *M* is a 3*d* transition metal such as Ni, Co, and Mn.  $\text{Li}MO_2$  has a layered structure with a space group of  $R\bar{3}m$ , whereas  $\text{Li}M_2O_4$  is a spinel-framework structure with a space group of  $Fd\bar{3}m$ .

structural environment.  $\chi$  measurements of  $LiCo_{1-x}Ni_xO_2$  with  $x \ge 0.85$  has revealed the presence of a small amount of Ni ions in the Li layer, although conventional X-ray diffraction (XRD) measurements fail to detect the Ni ions in the Li layers of these compounds.<sup>(8,19,20)</sup> In addition, the muon-spin rotation/relaxation ( $\mu$ SR) technique can be applied to research on lithium insertion materials, because an antiferromagnetic order is partially observed in stoichiometric LiCoO<sub>2</sub> below 30 K,<sup>(21)</sup> while LiCoO<sub>2</sub> was believed to be paramagnetic state down to 5 K according to  $\chi^{(22)}$  and <sup>7</sup>Li- nuclear magnetic resonance  $(NMR)^{(23)}$  measurements due to non-magnetic Co<sup>3+</sup> ions with S = 0  $(t_{2g}^{6}e_{g}^{0})$ . Here,  $\mu$ SR is very sensitive to local magnetic environments and is a powerful technique to detect both static and dynamic internal magnetic fields from 0.1 Oe to 100 kOe caused by nuclear- and electronic-magnetic moments.<sup>(24)</sup>

Figure 2 shows that the crystal structure of lithium insertion materials can be mainly classified into two categories; one is LiMO<sub>2</sub> with a layered structure  $(R\bar{3}m)$  (Fig. 2(a)) and the other is Li $M_2O_4$  with a spinel-framework structure  $(Fd\bar{3}m)$  (Fig. 2(b)), where M is a 3d transition metal, such as Co, Ni, and Mn. In the LiMO<sub>2</sub> structure, to which LiCoO<sub>2</sub>, LiNiO<sub>2</sub>, and  $LiCo_{1-x}Ni_xO_2$  (0 < x < 1) belong,  $Li^+$  ions and M ions occupy the octahedral 3b and 3a sites, respectively, in a cubic closed-packed (ccp) oxygen array. In contrast, the  $LiM_2O_4$  structure, which includes compositions such as  $\text{LiMn}_2\text{O}_4$ ,  $\text{Li}[\text{Li}_x\text{Mn}_{2-x}]\text{O}_4$  ( $0 \le x \le 1/3$ ), and  $Li[Ni_{1/2}Mn_{3/2}]O_4$ , the  $Li^+$  ions and M ions are situated on the tetrahedral 8a and octahedral 16d sites, respectively, in the *ccp* oxygen array. In  $LiMO_2$ ,  $Li^+$ ions can move in the x and y directions, i.e.,  $LiMO_2$  has two-dimensional (2D) ion channels, while  $LiM_2O_4$  has 3D channels. Furthermore, with respect to magnetism, LiMO<sub>2</sub> exhibits a 2D geometrical spin frustration, while  $LiM_2O_4$  has a 3D geometrical spin frustration. In this paper, we report on results from systematic  $\chi$ and  $\mu$ SR studies of these compounds to clarify the interrelationship between the electrochemical, structural, and magnetic properties of lithium insertion materials. In section 3.1, the electrochemical properties of the layered Li<sub>x</sub>CoO<sub>2</sub> and Li<sub>x</sub>NiO<sub>2</sub> compounds are correlated to a magnetic phase diagram combined with the change in crystal structure with x. In sections 3.2 and 3.3, respectively, the microscopic structural nature of the Li[Li<sub>x</sub>Mn<sub>2-x</sub>]O<sub>4</sub> and Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub> spinels are described to provide an understanding of the homogeneity/inhomogeneity of the sample through its microscopic magnetism. Finally, the difference between the layered  $\text{Li}_x \text{NiO}_2$  and the  $\text{Li}_x \text{Mn}_2 \text{O}_4$  spinel during the delithiation reaction is discussed in section 3.4.

# 2. Experimental

# 2.1 Sample Preparation

Powder samples of  $LiCo_{1-x}Ni_xO_2$  with  $0 \le x \le 1$ , <sup>(25-33)</sup> Li[Li<sub>x</sub>Mn<sub>2-x</sub>]O<sub>4</sub> with  $0 \le x \le 1/3$ , (34,35) Li[Mg<sub>x</sub>Mn<sub>2-x</sub>]O<sub>4</sub> with  $0 \le x \le 1/2$ , <sup>(36)</sup> and Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub> <sup>(37,38)</sup> were prepared by solid-state reaction. For the  $LiCo_{1-x}Ni_xO_2$ samples, a mixture of LiNO<sub>3</sub> (Li<sub>2</sub>CO<sub>3</sub> for x = 1), NiCO<sub>3</sub>, and CoCO<sub>3</sub> powders was well mixed and pressed into a pellet of 23 mm diameter and ca. 5 mm thickness. The pellet was then heated in the temperature (T) range between 750 and 900°C in an oxygen (in air for x = 1) flow for 12 h.<sup>(25-33)</sup> For the Li[Li<sub>x</sub>Mn<sub>2-x</sub>]O<sub>4</sub>, Li[Mg<sub>x</sub>Mn<sub>2-x</sub>]O<sub>4</sub>, and Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub> samples, a two-step solid-state reaction<sup>(15,39)</sup> was employed to obtain highly crystallized samples with an octahedral crystal habit. In the first step, the crystallization process is completed at high T around 1000°C, and then in the second step, the chemical composition is controlled precisely below 700°C. For the Li[Li<sub>x</sub>Mn<sub>2-x</sub>]O<sub>4</sub> samples with  $0 \le x \le 1/3$ , a reaction mixture of LiOH H<sub>2</sub>O and MnOOH (manganite) was heated at 1000°C in air for 12 h, and then oxidized at 700°C for x = 0, 600°C for x = 0.1, 550°C for x = 0.2in air for 12 h. Only for the x = 1/3 sample, the pellet was oxidized at 650, 600, 550, and 500°C in air for 24 h without cooling to room  $T^{(35)}$  For the Li[Mg<sub>r</sub>Mn<sub>2-r</sub>]O<sub>4</sub> samples with  $0 \le x \le 1/2$ , a mixture of LiOH·H<sub>2</sub>O, Mg(OH)<sub>2</sub>, and MnOOH was heated at 1000°C for 12 h, then oxidized at 700°C in an oxygen flow.<sup>(36)</sup> Two structural types of  $Li[Ni_{1/2}Mn_{3/2}]O_4$  were prepared;<sup>(37,38)</sup> "cation-disordered"  $Li[Ni_{1/2}Mn_{3/2}]O_4$ the was synthesized by heating a mixture of LiOH·H<sub>2</sub>O and nickel manganese hydroxide at 1000°C for 12 h, and the "cation-ordered"  $Li[Ni_{1/2}Mn_{3/2}]O_4$ , i.e.,  $Li[Ni_{1/2}Mn_{3/2}]O_4$  (P4<sub>3</sub>32), was prepared by annealing the cation-disordered Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub> below 700°C. The obtained powders were characterized using powder XRD (RINT-2200, Rigaku Co. Ltd., Japan) and inductively coupled plasma-atomic emission spectroscopy (ICP-AES, CIROS 120, Rigaku Co. Ltd., Japan).

The electrochemical reactivity was examined in a non-aqueous lithium cell. For preparation of the electrode, poly-vinylidene fluoride (PVdF) dissolved in N-methyl-2-pyrrolidone (NMP) solution was used as a binder. The black viscous slurry, consisting of 88 wt% active material, 6 wt% acetylene black, and 6 wt% PVdF, was cast on an aluminum foil with a blade. NMP was evaporated at 120°C for 30 min, and the electrode (Ø15 mm) was then dried under vacuum at 150°C for 12 h. The counter electrode (Ø19 mm) was prepared by pressing lithium metal onto a stainless steel substrate. Two sheets of porous polypropylene membrane (Celgard 2500) were used as a separator. 1 M LiPF<sub>6</sub> dissolved in ethylene carbonate (EC)/dimethyl carbonate (DMC) (3:7 volume ratio) solution was used as the electrolyte. For the electrochemical tests, the current applied to the cell was 0.5 (or 0.3) mA, which corresponds to a current density of ca. 0.28 (or 0.17)  $mA \cdot cm^{-2}$ .

Delithiated samples for the  $\chi$  and  $\mu$ SR measurements were prepared by two different methods; by electrochemical reaction in a non-aqueous lithium cell<sup>(26-29,32,33,37)</sup> and by chemical reaction.<sup>(40-42)</sup> For the electrochemical reaction, the pressed powder and a lithium metal sheet were used as working and counter electrodes, respectively. To avoid signals from the conducting additives and binder, the electrode was made entirely from the active material. For the chemical reaction, 2 g of LiNiO<sub>2</sub> (3.6 g of LiMn<sub>2</sub>O<sub>4</sub>) powder was immersed into 100 mL of HNO<sub>3</sub> solution and then stirred at room *T* for 24 h. After the acid treatment, the sample was filtered and dried at 40°C (60°C for LiMn<sub>2</sub>O<sub>4</sub>) in an air-oven.

# 2.2 Magnetic Measurements

DC-magnetic measurements were carried out using a superconducting quantum interference device (SQUID) magnetometer (MPMS, Quantum Design) in the T range between 5 and 700 K under a magnetic field  $H \le 55$  kOe. The magnetic measurements provide the equilibrium value of magnetization (M) in a sample.<sup>(43,44)</sup> The sample is magnetized under constant T and H, and T dependence of the magnetic susceptibility  $\chi$  (= *M*/*H*) and a magnetization curve M(H) are obtained. The sample was packed into two sheets of aluminum foil  $(20 \times 20 \text{ mm})$ , attached to the SQUID sample rod with a copper wire, and then finally installed into the sample chamber. The sample was firstly cooled to 5 K and a magnetic field (H = 10 kOe) was applied using the "no overshoot" mode, in which the field oscillation is suppressed. After adjusting the sample position to the center of the SQUID coils,

measurements were performed with movement of the sample position. For the delithiated samples, the sample was removed from the lithium cell in an argon-filled glovebox just before  $\chi$  measurements.

The µSR experiment was performed at TRIUMF in Canada, Paul Scherrer Institut (PSI) in Switzerland, and Rutherford Appleton Laboratory (RAL) in UK. A muon is an elementary particle with spin 1/2 and gyromagnetic ratio  $\gamma_{\rm u}/2\pi = 13.554$  kHz/Oe. When ca. 100% polarized muons are implanted into a sample, the muon spin precesses by the local magnetic field of the sample. The unstable muons soon decay into positrons (the muon lifetime is 2.2 µs). The decay positron is then emitted preferentially along the muon spin direction. By collecting several million positrons as a function of the evolution time, the time (t)dependence of the muon-spin polarization  $(A_0P(t))$  can be constructed, where  $A_0$  is the initial asymmetry and P(t) is the polarization function. Zero-field (ZF)- $\mu$ SR is a very sensitive method used to detect weak internal magnetism that arises due to ordered magnetic moments or random fields that are static or fluctuating with time. Weak-transverse-field (wTF)-µSR, which involves the application of an external magnetic field perpendicular to the initial muon spin, is suitable for investigating the presence/absence of magnetic transition T, and the volume fraction of paramagnetic phases in the sample. More details regarding µSR technique are reported elsewhere.<sup>(24,45)</sup> Approximately one gram of sample was pressed into a pellet (Ø15 mm diameter, ca. 1 mm thick) and placed in the sample holder of a cryostat. The delithiated samples were removed from the lithium cell to a sealed sample cell in a He-filled glove-box, and then the sample cell was placed onto the sample holder of the cryostat. After the µSR measurements, the delithiated sample was returned to the lithium cell to evaluate the open circuit voltage (OCV) and confirm the stability of the sample during the µSR measurement.

### 3. Results and Discussion

## 3.1 Magnetism of $\text{LiCo}_{1-x}\text{Ni}_x\text{O}_2$ with $0 \le x \le 1^{(25-33)}$

Both LiCoO<sub>2</sub> and LiNiO<sub>2</sub> adopt a layered structure with  $R\bar{3}m$  space group, so that LiCo<sub>1-x</sub>Ni<sub>x</sub>O<sub>2</sub> is a solid solution between LiCoO<sub>2</sub> and LiNiO<sub>2</sub> in the entire x range.<sup>(6-10)</sup> However, with respect to  $\mu$ SR, the magnetism of LiCoO<sub>2</sub> is very different from that of LiNiO<sub>2</sub>, in that long-range antiferromagnetic (AF) ordering is observed below 30 K, probably due to a charge disproportionation reaction of the non-magnetic  $\text{Co}^{3+}$  ions  $(2\text{Co}^{3+} \rightarrow \text{Co}^{2+} + \text{Co}^{4+})$ .<sup>(21)</sup> In contrast, no long-range magnetic ordering is observed for LiNiO<sub>2</sub>, but a fast spin-glass-like fluctuation in Li<sub>0.98</sub>Ni<sub>1.02</sub>O<sub>2</sub> is observed even at 2 K.<sup>(46)</sup> Considering the structural features of the Co<sub>1-x</sub>Ni<sub>x</sub>O<sub>2</sub> plane, cations are likely to become ordered, although it is not impossible, but very difficult, to detect the (short-range) ordering by XRD. Therefore, systematic µSR measurements of powder LiCo<sub>1-x</sub>Ni<sub>x</sub>O<sub>2</sub> samples were conducted to elucidate the microscopic magnetism.

**Figure 3** shows ZF- $\mu$ SR spectra for the LiCo<sub>1-x</sub>Ni<sub>x</sub>O<sub>2</sub> samples with x = 0, 0.25, 0.5, 0.75, and 1 at 1.8 K inthe time domain below (a) 10 and (b) 1 µs. The ZF- $\mu$ SR spectrum for LiCoO<sub>2</sub> (x = 0) shows mainly a slow relaxation with a broad minimum at ca. 4 µs, which is a typical Kubo-Toyabe<sup>(47)</sup> (KT) signal due to randomly oriented nuclear magnetic moments of <sup>7</sup>Li (4.24  $\mu_N$ ) and <sup>59</sup>Co (5.25  $\mu_N$ ). However, a fast relaxation signal appears in the early time domain below ca. 0.2 µs (see Fig. 3(b)), due to the formation of a static AF ordered phase below 30 K. On the other hand, the ZF-µSR spectra for samples with x = 0.25, 0.5, and 0.75 show a rapid relaxation without an oscillation in the time domain below ca. 0.3 µs, which suggests that the muon spins are depolarized by disordered magnetic moments of Ni<sup>3+</sup> ions with S = 1/2 ( $t_{2g}^{6} e_{g}^{1}$ ). The ZF-µSR spectrum for the x = 1 sample is so strongly damped, which



**Fig. 3** ZF- $\mu$ SR spectra for LiCo<sub>1-x</sub>Ni<sub>x</sub>O<sub>2</sub> samples with x = 0, 0.25, 0.5, 0.75, and 1 in the time domain below (a) 10 and (b) 1  $\mu$ s. The solid lines indicate the fitting results using Eq. (1). The top four ZF- $\mu$ SR spectra are shifted upwards by + 0.2 for clarity.

indicates that the Ni moments freeze in a highly disordered fashion, as in the case for  $\text{Li}_{0.98}\text{Ni}_{1.02}\text{O}_2$ .<sup>(46)</sup> As a result, the ZF- $\mu$ SR spectra for  $\text{LiCo}_{1-x}\text{Ni}_x\text{O}_2$  are well fitted by a combination of four signals; an exponentially relaxing cosine oscillation signal due to AF ordering for LiCoO<sub>2</sub>, a KT signal due to randomly oriented nuclear moments, an exponentially relaxing non-oscillatory signal due to localized disordered moments, and a zeroth-order Bessel function of the first kind  $J_0(\omega_{\mu}t)$ , which describes the fast relaxation behavior for LiNiO<sub>2</sub>:<sup>(25-28,30,32,33)</sup>

where  $A_{AF}$ ,  $A_{KT}$ ,  $A_{fast}$ , and  $A_{IC}$  are the asymmetries of the four signals,  $\lambda_{AF}$ ,  $\lambda_{fast}$ , and  $\lambda_{IC}$  are their relaxation rates,  $\omega_{AF}$  is the muon Larmor frequency,  $\phi$  is the initial phase of the precession,  $\Delta$  is the field distribution width of the local fields at the disordered sites, and v is the field fluctuation rate. When v = 0, a dynamic KT function,  $G^{\text{DGKT}}(t, \Delta, v)$ , is the static Gaussian KT function  $G_{zz}^{\text{KT}}(\Delta, t)$  given by<sup>(47)</sup>

$$G_{zz}^{KT} = 1/3 + 2/3(1 - \Delta^2 t^2) \exp(-\Delta^2 t^2/2) \cdots (2)$$

A linear relation is obtained in the log( $\lambda_{\text{fast}}$ ) versus x curve, where  $\lambda_{\text{fast}}$  increases exponentially with increasing x, which suggests a significant role of Ni<sup>3+</sup> moments on  $\lambda_{\text{fast}}$ .<sup>(30)</sup> In addition, the magnitudes of the spin-glass-like transition temperature  $T_{f_2}$  effective magnetic moment  $\mu_{\text{eff}}$ , and Curie-Weiss temperature  $\Theta_p$ , vary almost linearly with x,<sup>(31)</sup> which suggests that the change of magnetic properties with x in LiCo<sub>1-x</sub> Ni<sub>x</sub>O<sub>2</sub> is explained by an increase in the quantity of Ni<sup>3+</sup> ions with S = 1/2 ( $f_{2g}^6 e_g^1$ ). Thus, the Co<sup>3+</sup> and Ni<sup>3+</sup> ions are homogeneously distributed in the LiCo<sub>1-x</sub> Ni<sub>x</sub>O<sub>2</sub> lattice even in a few angstrom.<sup>(30)</sup>

Li<sub>x</sub>CoO<sub>2</sub> exhibits structural variation with x at ambient T (shown in later in Fig. 5(a)); as x decreases from 1, Li<sub>x</sub>CoO<sub>2</sub> consists of a mixture of two rhombohedral ( $R\bar{3}m$ ) phases for 0.95 > x ≥ 0.75, a rhombohedral phase for 0.75 > x ≥ 0.56 ( $R\bar{3}m$ ), a monoclinic phase (C2/m) for 0.56 > x ≥ 0.51, and finally a rhombohedral phase at x < 0.51 ( $R\bar{3}m$ ).<sup>(4,5)</sup> Moreover, the crystal structure of Li<sub>x</sub>NiO<sub>2</sub> is dependent on x at ambient T. As x decreases from 1, the rhombohedral  $(R\bar{3}m)$  phase is stable down to x = 0.75, whereas the monoclinic phase (C2/m) is stable in the x range between 0.75 and ca. 0.45. As x is decreased further, the rhombohedral  $(R\bar{3}m)$  phase appears again for  $0.45 > x \ge 0.25$ , and finally two rhombohedral  $(R\bar{3}m)$  phases coexist at x < 0.25.<sup>(7,48,49)</sup> In order to clarify the correlation between the structural and magnetic properties of Li<sub>x</sub>CoO<sub>2</sub> and Li<sub>x</sub>NiO<sub>2</sub>, the macro- and microscopic magnetism for the electrochemically delithiated Li<sub>x</sub>CoO<sub>2</sub> and Li<sub>x</sub>NiO<sub>2</sub>, samples were investigated using  $\chi$  and  $\mu$ SR measurements.

**Figure 4**(a) shows the *T* dependence of  $\chi$  for the  $\text{Li}_x \text{CoO}_2$  samples with  $1 \ge x \ge 0.1$ . The  $\chi(T)$  curves for the samples with x = 0.1 and 0.44 are almost *T*-independent down to ca. 50 K, which suggests that the samples are Pauli-paramagnetic. The  $\chi(T)$  curves for the samples with  $0.75 \ge x \ge 0.49$  also exhibit Pauli-paramagnetic behavior down to ca. 170 K, and then  $\chi$  suddenly decreases and reaches a broad minimum at ca. 100 K with further decrease in *T*. The cusp around 170 K was also reported for x = 0.7 and 0.95;<sup>(21)</sup> the cusp appears in a wide range of *x* between 0.95 and 0.5.<sup>(26,27)</sup> According to  $\chi$  measurements in both zero-field-cooling (ZFC) and field-cooling (FC) modes with H = 100 Oe and 10 kOe, the cusp around 170 K is not



**Fig. 4** (a) Temperature dependence of  $\chi$  and (b) ZF- $\mu$ SR spectra at 1.8 K for Li<sub>x</sub>CoO<sub>2</sub> samples with  $1 \ge x \ge 0.1$ .  $\chi$  was measured in FC mode with H = 10 kOe. The solid lines in (b) represent the fitting results from Eq. (3). The top six  $\chi(T)$  curves and five ZF- $\mu$ SR spectra are shifted upwards by  $+ 0.5 \times 10^{-3}$  and + 0.1, respectively, for clarity.

thought to be a typical ferromagnetic (FM), ferrimagnetic, and/or spin-glass-like transition.<sup>(27)</sup> In addition, wTF- $\mu$ SR measurements indicate that the x = 0.5 sample is in a PM state down to ca. 20 K.<sup>(27)</sup> Therefore, the cusp is thought to be a structural phase transition, a spin-state transition, and/or chargeordering. Recent low-T XRD measurements revealed a structural phase transition around 170 K.<sup>(29)</sup> Figure 4(b) shows the ZF- $\mu$ SR spectra for the Li<sub>x</sub>CoO<sub>2</sub> samples with  $1 \ge x \ge 0.12$  measured at 1.8 K. An oscillatory signal due to the formation of AF ordering disappears even for the x = 0.95 sample, and in turn, a slow relaxation signal due to the randomly oriented nuclear magnetism is observed for the x < 1 samples. The ZF- $\mu$ SR spectra for x < 1 is well fitted by a combination of a dynamic KT<sup>(47)</sup> function  $G^{\text{DGKT}}(t, \Delta, \nu)$  and an offset signal due to the Ag sample cell.

where  $A_{BG}$  is the asymmetry of the background signal and  $\lambda_{BG}$  is its relaxation rate. Note that a fast relaxation signal is observed only for the x = 0.5 sample in the time domain below 1 µs. However, the volume fraction of the fast relaxation signal is ca. 25%, even at 1.8 K, which indicates that most of the sample is in the PM state down to 1.8 K.

Figure 5 shows a schematic illustration of the (a) electrochemical reaction scheme and (b) magnetic phase diagram determined from  $\chi$  and  $\mu$ SR measurements for Li<sub>x</sub>CoO<sub>2</sub>. Static AF ordering is observed only for the x = 1 sample below 30 K, but the volume fraction is ca. 10%. All the  $Li_rCoO_2$  samples with x < 1 exhibit Pauli PM behavior even at 1.8 K. Thus, even if the average valence of Co ions and the crystal structure of  $\text{Li}_x \text{CoO}_2$  change with decreasing *x*, the magnetism of Li<sub>x</sub>CoO<sub>2</sub> does not vary dramatically. Note that the magnetism of Li<sub>x</sub>CoO<sub>2</sub> is quite different from those of  $A_x \text{CoO}_2$  (A = Na and K), although  $Na_x CoO_2^{(50,51)}$  and  $K_x CoO_2^{(52,53)}$  exhibit static AF ordering accompanied with structural phase transitions. The crystal structure of  $\text{Li}_x \text{CoO}_2$  with x < 0.25 belongs to a rhombohedral or monoclinic phase with the ccp structure, while those of Na<sub>x</sub>CoO<sub>2</sub> and K<sub>x</sub>CoO<sub>2</sub> are hexagonal close-packed (hcp) structures. This indicates that the arrangement of Co ions along the *c*-axis in  $Li_xCoO_2$  is different from those in  $Na_xCoO_2$  and  $K_x CoO_2$ ; in the former, Co ions locate at the center of the Co triangular lattice, but in the latter two, the Co ions locate at the same (x, y) position to those in the neighboring CoO<sub>2</sub> plane. Therefore, the stacking sequence along the c-axis is thought to be crucial to determine the formation of AF ordering in  $A_x$ CoO<sub>2</sub>.<sup>(25-27)</sup>

**Figure 6** shows the ZF- $\mu$ SR spectrum for the Li<sub>x</sub>NiO<sub>2</sub> sample with x = 0.75 at 1.8 K. The ZF- $\mu$ SR spectrum at 45 K exhibits KT behavior, which indicates that the sample is in a PM state (not shown). However, the ZF- $\mu$ SR spectrum at 1.8 K has a damped oscillation, which indicates the formation of static AF ordering. The fit using a cosine oscillation (exp( $-\lambda t$ )cos( $\omega_{\mu} + \phi$ )) yields a delay of the initial phase ( $\phi$ ) by ca.  $-40^{\circ}$ , which is physically meaningless. Thus, the ZF- $\mu$ SR spectrum is fitted by a zeroth-order Bessel function  $J_0(\omega_{\mu}t)$ , as in the case for LiNiO<sub>2</sub>, which describes the muon polarization evolution in an incommensurate (IC-) field distribution.

where  $A_{\rm IC}$ ,  $A_{\rm fast}$ , and  $A_{\rm slow}$  are the asymmetries of the three signals and  $\lambda_{\rm IC}$ ,  $\lambda_{\rm fast}$ , and  $\lambda_{\rm slow}$  are their relaxation rates. As *T* decreases from 35 K,  $f_{\rm IC}(=\omega_{\rm IC}/2\pi)$  increases



Fig. 5 Schematic illustration of (a) electrochemical reaction scheme and (b) magnetic phase diagram for  $\text{Li}_x\text{CoO}_2$ .  $T_m$  and  $T_N$  are magnetic transition temperatures determined from  $\chi$  and  $\mu$ SR measurements, respectively. AF and PARA denote antiferromagnetism and paramagnetism, respectively.

rapidly with decrease in the  $df_{IC}/dT$  slope, and finally reaches ca. 30 MHz at 1.8 K, as expected for the ordering parameter of the AF transition. Considering the "1/3" tail component due to a polycrystalline sample ( $A_{fast} + A_{slow}$ ), the normalized  $A_{IC}$  suggests that almost all the sample enters the AF phase below 35 K. Note that the ZF-µSR spectrum for LiCo<sub>0.25</sub>Ni<sub>0.75</sub>O<sub>2</sub> exhibits a spin-glass-like disordered magnetism (see Fig. 3), although the spin concentration on the twodimensionally triangular lattice in Li<sub>0.75</sub>NiO<sub>2</sub> is the same as that in LiCo<sub>0.25</sub>Ni<sub>0.75</sub>O<sub>2</sub>; Ni<sup>3+</sup> ions are magnetic with S = 1/2 ( $t_{2g}^{6}e_{g}^{1}$ ), while Ni<sup>4+</sup> and Co<sup>3+</sup> ions are nonmagnetic with S = 0 ( $t_{2g}^{6}e_{g}^{0}$ ).

The oscillatory signal is also observed for the  $\text{Li}_x \text{NiO}_2$  samples with  $x \ge 0.6$ , which suggests the formation of static AF ordering. Although the AF structure is not fully understood at present, A-type AF ordering, i.e., FM in the plane, but AF between the plane, is most reasonable, as in the case for  $\text{NaNiO}_2$ .<sup>(54)</sup> This is because the Curie-Weiss temperature  $\Theta_p$ , estimated from the  $\chi(T)$  curves ranges between + 25 and + 60 K for the  $x \ge 0.6$  samples, which suggests that the predominant interaction between Ni moments is FM.

The schematic magnetic phase diagram for  $\text{Li}_x \text{NiO}_2$ is finally established from the  $\chi$  and  $\mu$ SR measurements (see **Fig. 7**).<sup>(32,33)</sup> A dome-shaped AF phase region exists in the range of *x* between 1 and ca. 0.55, whereas the spin-glass-like phase appears at 0.55  $\geq x \geq 0.1$ . Note that  $\chi$  measurements provide no



**Fig. 6** ZF- $\mu$ SR spectrum for the Li<sub>x</sub>NiO<sub>2</sub> sample with x = 0.75 at 1.8 K. The solid line indicates the fitting result from Eq. (4). An oscillatory signal suggests the formation of static AF ordering in the sample. The temperature dependence of normalized weak-transverse-field asymmetry ( $N_{\text{ATF}}$ ) is also shown in the inset.  $T_{\text{N}}^{\text{mid}}$  is the temperature at which  $N_{\text{ATF}} = 0.5$ .

information on the change in magnetic nature of  $Li_xNiO_2$  with x; the magnitude of the spin-glass-like temperature  $T_f$  decreases almost linearly with decreasing x. Such a discrepancy between  $\chi$  and  $\mu$ SR measurements is also observed for stoichiometric  $LiCoO_2^{(21,25-27)}$  and low-dimensional systems such as  $Ca_3Co_2O_5$ .<sup>(55)</sup> This is because muons are influenced by the magnetic fields from nearest neighbors and are especially sensitive to short-range magnetic ordering that often appears in low-dimensional systems, whereas  $\chi$  measurements mainly detect long range magnetic ordering. Furthermore, µSR measures fluctuating magnetic order/disorder on a muon timescale  $(10^{4}-10^{12} \text{ s}^{-1})$ , while (dc)- $\chi$  provides static information. Although the correlation between the solid-state electrochemistry and magnetism of Li<sub>x</sub>NiO<sub>2</sub> is currently unclear, the present results demonstrate that µSR measurements are suitable to study the change in the physical/structural properties of Li<sub>x</sub>NiO<sub>2</sub> during the charge/discharge reaction.

# 3.2 Magnetism of $Li[Li_xMn_{2-x}]O_4$ with $0 \le x \le 1/3^{(34,35)}$

In the crystal lattice of the  $Li[Li_xMn_{2-x}]O_4$  (LMO)



**Fig. 7** Schematic illustrations of (a) the electrochemical reaction scheme and (b) magnetic phase diagram for  $\text{Li}_x \text{NiO}_2$ .  $T_f$  and  $T_N^{\text{mid}}$  are magnetic transition temperatures determined from  $\chi$  and  $\mu$ SR measurements, respectively. PARA, AF, and SG denote paramagnetic, antiferromagnetic, and spin-glass-like phases, respectively.

spinel with space group  $Fd\bar{3}m$ , non-magnetic Li<sup>+</sup> ions locate at both tetrahedral 8*a* and 16*d* sites, while magnetic Mn<sup>3+</sup> ions with  $S = 2(t_{2g}^{3}e_{g}^{1})$  and Mn<sup>4+</sup> ions with  $S = 3/2(t_{2g}^{3}e_{g}^{0})$  occupy the octahedral 16*d* sites. The excess Li<sup>+</sup> ions at the 16*d* sites (*x*) not only dilute the magnetic interaction between Mn ions, but also increase the average valence of Mn ions ( $V_{Mn}^{ave}$ );  $V_{Mn}^{ave} =$ 3.5 for LiMn<sub>2</sub>O<sub>4</sub>, and as *x* increases from 0,  $V_{Mn}^{ave}$ increases in proportion to *x*, and reaches 4 for Li[Li<sub>1/3</sub>Mn<sub>5/3</sub>]O<sub>4</sub>. We have performed  $\chi$  and ZF- $\mu$ SR measurements for samples with  $0 \le x \le 1/3$  to elucidate the structural and physical properties of LMO. **Figures 8**(a) and (b) show the *T* dependence of the field distribution width  $\Delta$ , and the muon fluctuation



Fig. 8 Temperature dependence of (a) field distribution width ( $\Delta$ ), (b) field fluctuation rate (v), and (c) inverse magnetic susceptibility ( $\chi^{-1}$ ) for Li[Li<sub>x</sub>Mn<sub>2-x</sub>]O<sub>4</sub> samples with x = 0, 0.05, 0.1, and 0.15. The data was obtained by fitting the ZF- $\mu$ SR spectra using a dynamic KT function.  $\chi$  was measured in FC mode with H = 10 kOe.  $T_{JT}$ represents the transition temperature due to the cooperative Jahn-Teller (JT) distortion of Mn<sup>3+</sup> ions with S = 2 ( $t_{2g}^3 e_g^1$ ).

rate v, for LMO samples with x = 0, 0.05, 0.1, and0.15. Here, the values of  $\Delta$  and v are obtained by fitting the ZF- $\mu$ SR spectra with a dynamic KT<sup>(47)</sup> function  $G^{\text{DGKT}}(t, \Delta, v)$ . For the x = 0 sample, as *T* increases from 100 K,  $\Delta$  remains almost constant (ca. 0.17  $\mu$ s<sup>-1</sup>) up to ca. 280 K, then suddenly drops to ca. 0.1  $\mu$ s<sup>-1</sup> with further increase in T. On the other hand, v for the x = 0 sample reaches a maximum around 280 K, and then increases with further increase in T. Stoichiometric LiMn<sub>2</sub>O<sub>4</sub> is known to exhibit a structural phase transition from a high-T cubic phase (Fd3m) to a low-T orthorhombic (Fddd) phase at  $T_{\rm JT}$  $\sim$  280 K, induced by a cooperative Jahn-Teller (JT) distortion of Mn<sup>3+</sup> ions.<sup>(56-58)</sup> Furthermore, the  $\chi^{-1}(T)$ curve for the x = 0 sample exhibits a small cusp at ca. 280 K, as shown in Fig. 8(c), due to orbital ordering of  $Mn^{3+}$  ions at  $T_{IT}$ . Thus, the sudden decrease in  $\Delta$  and the peak of the v(*T*) curve around 280 K are naturally assigned as to the JT transition. This can be explained as the consequence of a critical slowing down toward  $T_{\rm JT}$  due to spin-phonon interaction.<sup>(59)</sup> It should be noted that the sudden decrease in  $\Delta$  and the peak of the v(T) curve are still observed even for the x = 0.15 sample, although there are no anomalies in the  $\chi^{-1}(T)$  curve. Therefore,  $\mu$ SR detects the appearance of a short-range cooperative JT distortion even in the sample with x = 0.15,<sup>(34)</sup> while macroscopic analyses such as XRD and differential scanning calorimetry (DSC) show that  $T_{\rm JT}$  disappears at around x = 0.035.<sup>(56)</sup>

**Figure 9** shows the charge and discharge curves of a lithium cell with the x = 1/3 sample. We assume that the theoretical charge/discharge capacity ( $Q_{\text{theo}}(x)$ ) for LMO with x > 0 is determined by the following reaction:

where  $Q_{\text{theo}}(x)$  in mAh g<sup>-1</sup> is given by

$$Q_{\text{theo}}(x) = Q_{\text{theo}}(\text{LiMn}_2\text{O}_4) \times (1 - 3x) \times \frac{M(\text{LiMn}_2\text{O}_4)}{M(x)},$$
  
.....(6)

where  $Q_{\text{theo}}(\text{LiMn}_2\text{O}_4)$  is the theoretical charge/ discharge capacity of  $\text{LiMn}_2\text{O}_4$  (= 148 mAh·g<sup>-1</sup>), and  $M(\text{LiMn}_2\text{O}_4)$  and M(x) are the molecular weights of  $\text{LiMn}_2\text{O}_4$  and LMO with x > 0, respectively. This means that  $Q_{\text{theo}}(x)$  decreases linearly with increasing x, and finally reaches 0 mAh g<sup>-1</sup> at x = 1/3 (see Fig. 9(b)). However, as shown in Fig. 9(a), approximately 46 mAh g<sup>-1</sup> of rechargeable capacity is obtained for the x = 1/3 sample. Moreover, a difference between  $Q_{\text{theo}}(x)$  and the charge capacity at the fist cycle ( $Q_{\text{cha}}$ ) is evident at x > 0.2 (see Fig. 9(b)). The  $\mu$ SR signal roughly corresponds to the volume fraction of the magnetic phases in the sample; therefore,  $\mu$ SR measurements were conducted for the x = 1/3 and Li<sub>2</sub>MnO<sub>3</sub> samples to clarify the homogeneity/ inhomogeneity of the x = 1/3 sample through its microscopic magnetism.

**Figure 10** shows ZF- $\mu$ SR spectra measured at 1.8 K for the LMO samples with x = 0, 0.1, 0.2, and 1/3. The ZF- $\mu$ SR spectra for the samples with  $x \ge 0.2$  lack an oscillatory signal, but pose a first minimum at around  $t = 0.015 \,\mu$ s, which indicates a spin-glass-like freezing of the Mn moments at low *T*. On the other hand, a clear oscillation with an oscillation frequency f = 42.3(3)

MHz is observed for the x = 1/3 sample. XRD measurements indicate that the Li<sub>2</sub>MnO<sub>3</sub> phase coexists in the x = 1/3 sample and that the weight fraction of the Li<sub>2</sub>MnO<sub>3</sub> phase ( $W_p$ (Li<sub>2</sub>MnO<sub>3</sub>)) in the x = 1/3 sample is 11.0%. Furthermore, as shown in Fig. 10(e), the ZF- $\mu$ SR spectrum for the Li<sub>2</sub>MnO<sub>3</sub> sample has an oscillation signal with an oscillation frequency f = 42.2(1) MHz. The oscillation is, thus, caused by the Li<sub>2</sub>MnO<sub>3</sub> phase in the x = 1/3 sample. Figure 11 shows the T dependence of normalized wTF asymmetries  $(N_{\text{ATF}})$  for the LMO samples with x = 0, 0.1, 0.2, and 1/3 together with the result for  $Li_2MnO_3$ . Here,  $N_{\rm ATF}$  corresponds to the volume fraction of PM phases in the sample; when  $N_{\text{ATF}} = 1$ , the entire sample is in a PM state, whereas when  $N_{\text{ATF}} = 0$ , the sample is in a magnetic phase such as FM, AF, or ferrimagnetic, spin-glass-like phases. A step-like decrease in  $N_{\text{ATF}}$ from 1 to 0 for the samples with  $x \le 0.2$  indicates the existence of a sharp magnetic transition for these samples. On the contrary, as T decreases from 50 K,



**Fig. 9** (a) Charge and discharge curves of a lithium cell with  $\text{Li}[\text{Li}_x\text{Mn}_{2-x}]O_4$  (LMO) at x = 1/3. The cell was operated in the voltage range between 3 and 5 V at a current density of 0.17 mA·cm<sup>-2</sup> at 25°C. A comparison of the theoretical charge/discharge capacity ( $Q_{\text{theo}}$ ) and the experimental charge capacity at the first cycle ( $Q_{\text{cha}}$ ) is shown in (b). Note that  $Q_{\text{theo}}$  should be 0 mAh·g<sup>-1</sup> at x = 1/3 if it is assumed that the electrochemical reaction proceeds according to Eq. (5).





 $N_{\text{ATF}}$  for the x = 1/3 sample decreases slightly around 36 K, then gradually decreases with further lowering of *T*.  $N_{\text{ATF}}$  for the Li<sub>2</sub>MnO<sub>3</sub> sample exhibits a step-like decrease at 36 K due to the formation of AF ordering;<sup>(60)</sup> therefore, the small decrease at 36 K in the x = 1/3 sample is caused by the magnetic transition of Li<sub>2</sub>MnO<sub>3</sub>.

The x = 1/3 compound has been assigned as a mixture of a Li[Li<sub>x</sub>Mn<sub>2-x</sub>]O<sub>4</sub> phase and a Li<sub>2</sub>MnO<sub>3</sub> phase;<sup>(61-63)</sup> the actual chemical formula, especially at x > 0.2, is represented by

where

 $\omega = (x - z)/(1 - z) \cdots (8)$ 

The chemical formula for the remaining spinel phase of the x = 1/3 sample is calculated to be  $\text{Li}[\text{Li}_{0.21}\text{Mn}_{1.79}]\text{O}_4$  ( $\omega = 0.124$ ) using Eqs. (7) and (8) and  $W_p(\text{Li}_2\text{MnO}_3) = 11.0\%$ . Figure 11 shows that the x = 1/3 sample has a large magnetic transition width ( $\Delta T_m \sim 28$  K) compared to those for the x = 0.2 ( $\Delta T_m \sim 5$  K) and  $\text{Li}_2\text{MnO}_3$  ( $\Delta T_m \sim 2$  K) samples. This indicates that the value of  $\omega$  in the  $\text{Li}[\text{Li}_x\text{Mn}_{2-x}]\text{O}_4$ lattice is microscopically different, although XRD and neutron diffraction measurements have indicated that  $\text{Li}[\text{Li}_{x-\omega}\text{Mn}_{2-x+\omega}]\text{O}_4$  is single-phase.<sup>(61-63)</sup> In other words, it is most likely that the inhomogeneous distribution of Li ions at the 16*d* sites correlates to the abnormal charge/discharge capacity for the x = 1/3



**Fig. 11** Temperature dependence of the normalized wTFasymmetries ( $N_{ATF}$ ) for Li[Li<sub>x</sub>Mn<sub>2-x</sub>]O<sub>4</sub> with x = 0, 0.1, 0.2, and 1/3, together with that for Li<sub>2</sub>MnO<sub>3</sub>.

sample.<sup>(35)</sup> As pointed out by Paulsen and Dahn, the number of phases that can co-exist in the Li-Mn-O compound is estimated to be two, if the Gibbs phase rule is applied.<sup>(64)</sup> However, such multiple phases in the x = 1/3 sample suggest that rate of Eq. (7) is too slow to reach the thermodynamic equilibrium state. The inconsistency with the Gibbs phase rule prediction is also observed for fully delithiated  $Li_x NiO_2$  with  $x \le x$ 0.1; at least four different phases are present in the sample.<sup>(41,65,66)</sup> The composite compounds of  $x \text{Li}_2 \text{MnO}_3$  (1-x)LiMn<sub>2</sub>O<sub>4</sub><sup>(67)</sup> and/or  $x \text{Li}_2 \text{MnO}_3$  (1-x)LiMO<sub>2</sub> with M = Co, Ni, and Mn<sup>(68,69)</sup> have recently been promising as positive electrode materials for highenergy density LIBs. Cation-ordering between Li and Mn ions, such as in the  $Li_2MnO_3$  (Li[ $Li_{1/3}Mn_{3/2}$ ]O<sub>2</sub>) phase, is present in these compounds; therefore,  $\mu$ SR measurements would be useful to investigate the local structural environment in these compounds.

## 3.3 Magnetism of Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub><sup>(36-38)</sup>

Among the lithium manganese oxide spinels, Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub> is promising as a future positive electrode material, due to its high operating voltages around 4.7 V vs. Li<sup>+</sup>/Li.<sup>(14-16)</sup> Stoichiometric  $Li[Ni_{1/2}Mn_{3/2}]O_4$  (CO-LNMO) exhibits a 1:3 cationordering (CO) between Ni<sup>2+</sup> and Mn<sup>4+</sup> ions, which results in a superlattice structure that belongs to the  $P4_332$  space group. However, cation-disordering (CDO) Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub> (CDO-LNMO) is easily formed depending on the reaction conditions.<sup>(14-16,39)</sup> The electrochemical properties of CDO-LNMO are different from those of CO-LNMO, (14-16,39) so that a quantitative indicator to identify the Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub>  $(P4_332)$  phase would be useful for optimization of the synthesis conditions. Therefore,  $\chi$  measurements were conducted for both CO-LNMO and CDO-LNMO samples to clarify the inter-relationship between the magnetic and electrochemical properties of  $Li[Ni_{1/2}Mn_{3/2}]O_4.$ 

**Figure 12**(a) shows charge/discharge curves of lithium cells with both CO-LNMO and CDO-LNMO samples. The charge/discharge curves for the CO-LNMO sample have a very flat operating voltage around 4.7 V. The rechargeable capacity in the voltage range between 3 and 5 V is 134 mAh·g<sup>-1</sup>, which corresponds to ca. 92% of the theoretical capacity calculated from the formula weight of Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub>. In contrast, the charge/discharge curves for the CDO-LNMO sample are divided into

three distinct regions; a continuous change in voltage below ca. 4.6 V and two plateaus at around 4.6 and 4.7 V. The Fourier transform infrared (FTIR) spectrum for CO-LNMO indicates the existence of cationordering in the sample (see Fig. 12(b)). On the basis of factor group analysis,<sup>(70)</sup> IR active vibration modes for the  $Fd\bar{3}m$  space group are predicted to be 4 ( $4F_{1u}$ ), while those for the  $P4_332$  group are expected to be 21 ( $21F_1$ ). At least eight or more absorption bands appear only for the CO-LNMO sample, which indicates that its space group symmetry is lower than  $Fd\bar{3}m$ . Comparing the results reported previously for Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub>,<sup>(14-16,39)</sup> CO-LNMO and CDO-LNMO samples are assigned as Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub> ( $P4_332$ ) and cation-disordering Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub>, respectively.

**Figure 13** shows the *T* dependence of (a)  $\chi$ , (b)  $\chi^{-1}$ , and (c)  $d\chi^{-1}/dT$  for the CO-LNMO and CDO-LNMO samples measured in FC mode with H = 10 kOe.  $\chi$  for both samples rapidly increase below ca. 130 K with decreasing *T*, which suggests the appearance of

spontaneous magnetization. Above 200 K,  $\chi^{-1}$  increase with increasing *T* with a change in the  $d\chi^{-1}/dT$  slope. For a PM state, the Curie-Weiss law in the general form is written as

$$\chi = \frac{N\mu_{\text{eff}}^2}{3k_{\text{B}}(T - \Theta_{\text{p}})} + \chi_0, \quad \dots \quad \dots \quad \dots \quad (9)$$

where *N* is the number density of Ni and Mn ions,  $\mu_{eff}$  is the effective magnetic moment of Ni and Mn ions,  $k_B$  is Boltzmann's constant, *T* is the absolute temperature,  $\Theta_p$  is the Curie-Weiss temperature, and  $\chi_0$  is the temperature-independent susceptibility. Figure 13(c) shows that  $d\chi^{-1}/dT$  is almost *T*-independent for both samples. The values of  $\mu_{eff}$  and  $\Theta_p$  are therefore calculated by fitting the  $\chi(T)$  curves in the *T* range between 500 and 700 K, which gives  $\mu_{eff} = 3.78(1) \mu_B$  and  $\Theta_p = -67(3)$  K for the CDO-LNMO sample, and  $\mu_{eff} = 3.50(1) \mu_B$  and  $\Theta_p = +7.8(2)$  K for the CO-LNMO sample. If we assume that Ni<sup>2+</sup> ions are in the  $S = 1 (t_{2g}^6 e_g^2)$  state, Mn<sup>4+</sup> ions are in the S = 3/2



Fig. 12 (a) Charge and discharge curves of lithium cells with both CDO-LNMO and CO-LNMO. The cells were operated in the voltage range between 3 and 5 V at a current density of 0.28 mA·cm<sup>-2</sup> at 25°C. (b) FTIR spectra for the CDO-LNMO and CO-LNMO samples. The more than eight absorption bands in (b) indicate that the space group symmetry of CO-LNMO is lower than  $Fd\bar{3}m$ .



Fig. 13 Temperature (*T*) dependence of (a)  $\chi$ , (b)  $\chi^{-1}$ , and (c) the slope of  $\chi^{-1}$  (d $\chi^{-1}$ /d*T*) for the CDO-LNMO and CO-LNMO samples.  $\chi$  was measured in FC mode with H = 10 kOe. The solid line in (c) represents the predicted effective magnetic moment ( $\mu_{eff}^{pre}$ ) calculated assuming that Ni<sup>2+</sup> ions are in the S = 1 ( $t_{2g}^{6}e_{g}^{2}$ ) state, Mn<sup>4+</sup> ions are in the S = 3/2 ( $t_{2g}^{3}e_{g}^{0}$ ) state, and g = 2.

 $(t_{2g}^{a}e_{g}^{0})$  state, and the gyromagnetic constant g = 2, then the spin-only effective magnetic moment  $(\mu_{eff}^{pre})$  for  $\text{Li}[\text{Ni}_{1/2}^{2+}\text{Mn}_{3/2}^{4+}]O_{4}$  is predicted to be 3.64  $\mu_{\text{B}}$ . The  $\mu_{eff}$ obtained for both samples are almost consistent with  $\mu_{eff}^{pre}$ , although  $\mu_{eff}$  for CDO-LNMO is slightly larger than that for CO-LNMO. Here, we wish emphasize that the  $\chi(T)$  curves typically reported for  $\text{Li}[\text{Ni}_{1/2}\text{Mn}_{3/2}]O_{4}$  below 400 K<sup>(71-73)</sup> provide an incorrect estimation of both  $\mu_{eff}$  and  $\Theta_{p}$ .

**Figure 14**(a) shows the *T* dependence of  $\chi$  for the CDO-LNMO and CO-LNMO samples in both ZFC and FC modes with H = 100 Oe. Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub> is already known to undergo a ferrimagnetic transition at around  $T_{\rm C} = 130$  K; the spin arrangements of both Ni<sup>2+</sup>-Ni<sup>2+</sup> and Mn<sup>4+</sup>-Mn<sup>4+</sup> ions are FM, but that of Ni<sup>2+</sup>-Mn<sup>4+</sup> ions is AF.<sup>(74)</sup> As *T* decreases from 150 K,  $\chi_{\rm FC}$  for the CO-LNMO sample rapidly deviates from  $\chi_{\rm ZFC}$  at ca. 130 K, which indicates a sharp ferrimagnetic transition. In contrast, the magnetic behavior for CDO-



Fig. 14 (a) Temperature dependence of  $\chi$  for the CDO-LNMO and CO-LNMO samples measured in ZFC and FC modes with H = 100 Oe. (b) M as a function of H for the CDO-LNMO and CO-LNMO samples. The solid lines indicate the predicted spin-only net magnetic moment ( $\mu_{eff}^{pre}$ ) calculated assuming that Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub> is ferrimagnetic, the spin arrangements of both Ni<sup>2+</sup>-Ni<sup>2+</sup> and Mn<sup>4+</sup>-Mn<sup>4+</sup> ions are FM, but that of Ni<sup>2+</sup>-Mn<sup>4+</sup> ions is AF.

LNMO is very different from that for CO-LNMO and is classified as P-type ferrimagnetism.<sup>(43)</sup> That is, as *T* decreases from 150 K,  $\chi_{ZFC}$  starts to deviate from  $\chi_{FC}$  below ca. 120 K and reaches a broad maximum at ca. 50 K, which suggests that a ferrimagnetic contribution except for the interaction between Ni<sup>2+</sup> and Mn<sup>4+</sup> ions, and/or a spin-glass-like contribution occur in the sample. Figure 14(b) shows that the *M*-*H* curve for the CO-LNMO sample at 5 K exhibits a typical loop of a soft ferromagnet, i.e., *M* rapidly increases with increasing *H* and levels off at 18.5 × 10<sup>3</sup> emu·mol<sup>-1</sup>, even at  $H \le 5$  kOe. If we assume that Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub> is ferrimagnetic, the spin-only net magnetic moment ( $\mu_{eff}^{pre}$ ) is calculated to be 3.5  $\mu_{B}$  using the following relation:

$$\mu_{\rm net}^{\rm pre} = S_{\rm Mn} \times g \times 3/2 \cdot S_{\rm Ni} \times g \times 1/2 \quad \cdots \quad \cdots \quad (10)$$

where  $S_{\rm Mn} = 3/2$ ,  $S_{\rm Ni} = 1$ , and g = 2. The net magnetic moment ( $\mu_{\rm net}$ ) for the CO-LNMO sample at H = 55kOe (= 3.31  $\mu_{\rm B}$ ) is very close to  $\mu_{\rm eff}^{\rm pre}$  (= 3.5  $\mu_{\rm B}$ ). Although *M* for the CDO-LNMO sample does not saturate even at H = 55 kOe,  $\mu_{\rm net}$  is calculated to be 2.40  $\mu_{\rm B}$  from *M* at H = 55 kOe.

It is difficult to identify  $Li[Ni_{1/2}Mn_{3/2}]O_4$  (P4<sub>3</sub>32) from the CDO-LNMO phase using  $\mu_{eff}$ , because  $\mu_{eff}$  = 3.78(1)  $\mu_B$  for CDO-LNMO and  $\mu_{eff} = 3.50(1) \mu_B$  for CO-LNMO. However, the M-H curve clearly reveals a characteristic feature of  $Li[Ni_{1/2}Mn_{3/2}]O_4$  (P4<sub>3</sub>32). The M-H curve for CO-LNMO has an FM hysteresis with a saturation magnetization  $(M_s) \sim 3.31 \mu_B$ . This value is almost consistent with  $\,\mu_{\text{eff}}^{\text{pre}}$  (= 3.5  $\mu_{B}).$  Here,  $M_{\rm s}$  for Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub> were also reported by several authors:  $19.2 \times 10^3$  emu·mol<sup>-1</sup> ( $\approx 3.44 \mu_B$ ) at 5 K,<sup>(71)</sup>  $17.3 \times 10^3$  emu mol<sup>-1</sup> ( $\approx 3.10 \,\mu_B$ ) at 2 K,<sup>(72)</sup> and 16.5 ×  $10^3$  emu mol<sup>-1</sup> ( $\approx 2.96 \mu_B$ ) at 4 K.<sup>(73)</sup> Although there were no electrochemical data in the latter two reports, the charge/discharge curves for the former  $Li[Ni_{1/2}Mn_{3/2}]O_4$  showed a rechargeable capacity above 130 mAh  $g^{-1}$  with a flat operating voltage at around 4.7 V.<sup>(71)</sup> Figure 14(b) shows that M at H =55 kOe for CDO-LNMO is decreased to ca.  $13.4 \times 10^3$ emu mol<sup>-1</sup> ( $\approx 2.40 \ \mu_B$ ). Therefore, the discrepancy between the observed  $\mu_{net}$  and  $\mu_{eff}^{pre}$  should be attributed to the cation-disordering of Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub>, although this has not been claimed in the previous reports on the magnetism of Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub>.<sup>(71-73)</sup> In other words, we can quantitatively examine the degree of cationordering in the Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub> sample using  $\mu_{net}$ ,<sup>(38)</sup>

as in the XRD analysis of LiNiO<sub>2</sub> for which the integrated XRD peak ratio of I(003)/I(104) is a good indicator for the occupancy of Ni ions in the Li layers.<sup>(7)</sup> It should be noted that the highly crystallized Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub> compound was synthesized by a two-step solid-state reaction; well cation-ordering in Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub> is prepared by annealing the cation-disordering Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub> compound.<sup>(15,39)</sup> To produce a large amount of Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub> in the future, it is important to identify the quality of Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub> before measuring the electrochemical properties, and  $\chi$  measurements are expected to be a powerful tool for such a purpose.

Besides LIB applications, Li[Li<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub> (P4<sub>3</sub>32) is a subject of considerable interest with respect to magnetism, because Ni and Mn ions form a threedimensional array of corner-sharing tetrahedral, and thus satisfy one of the conditions for geometrical frustration. Figure 14(b) shows an M-H curve for the delithiated Li<sub>0.05</sub>[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub> sample, which is prepared from the CO-LNMO sample bv electrochemical reaction.<sup>(37)</sup> Although a small FM component is observed within  $H \le 5$  kOe, M increases almost linearly with H up to 55 kOe. The M(H) curve for  $Li_{0.05}[Ni_{1/2}Mn_{3/2}]O_4$  is very similar to that for  $\lambda$ - $MnO_2$  (Li<sub>0</sub>Mn<sub>2</sub>O<sub>4</sub>),<sup>(37)</sup> so that the Li<sub>0.05</sub>[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub> sample is considered to be in a PM or AF state even at 5 K.

The ionic distribution and spin arrangement of  $\text{Li}_{0}[\text{Ni}_{1/2}^{4+}\text{Mn}_{3/2}^{4+}]O_4$  are the same as those for  $\text{Li}[\text{Mg}_{1/2}^{2+}\text{Mn}_{3/2}^{4+}]O_4^{(36)}$  and  $\text{Li}_{1/2}\text{Zn}_{1/2}[\text{Li}_{1/2}^{+}\text{Mn}_{3/2}^{4+}]O_4^{(74,75)}$  the Mn<sup>4+</sup> ions are located at the 12*d* sites of the spinel lattice with *P*4<sub>3</sub>32 space group, and the Ni<sup>4+</sup>, Mg<sup>2+</sup>, and Li<sup>+</sup> ions are non-magnetic. Both *M*-*H* curves for  $\text{Li}[\text{Mg}_{1/2}\text{Mn}_{3/2}]O_4$  (*P*4\_332) and  $\text{Li}_{1/2}\text{Zn}_{1/2}[\text{Li}_{1/2}\text{Mn}_{3/2}]O_4$  (*P*2<sub>1</sub>3) exhibit soft FM behavior below  $T_{\rm C} = 20 \text{ K}^{(36)}$  and  $T_{\rm C} = 22 \text{ K}^{(75)}$ , respectively; therefore, the *M*(*H*) curve for the *x* = 0.05 sample is very different from those for Li[Mg\_{1/2}\text{Mn}\_{3/2}]O\_4 and Li<sub>1/2</sub>Zn<sub>1/2</sub>[Li<sub>1/2</sub>Mn<sub>3/2</sub>]O\_4.

The different magnetic behavior between  $Li_{0.05}[Ni_{1/2}Mn_{3/2}]O_4$  and  $Li[Mg_{1/2}Mn_{3/2}]O_4$  (and  $Li_{1/2}Zn_{1/2}[Li_{1/2}Mn_{3/2}]O_4$ ) could be explained by the dependence of magnetic interactions on the cubic lattice parameter  $a_c$ , i.e., the distance between  $Mn^{4+}$  ions ( $r_{Mn-Mn}$ ). If we consider only the first nearest neighbor (nn) coupling constant ( $J_1$ ) and ignore the coupling between the second and higher nn, then the 90° superexchange  $Mn^{4+}-O^2-Mn^{4+}$  ( $J_{1,s}$ ) interaction should be FM, whereas direct  $Mn^{4+}-Mn^{4+}$  ( $J_{1,d}$ ) interaction should be AF.<sup>(76)</sup> This means that the

magnetic behavior of  $\text{Li}_{x}[M_{1/2}\text{Mn}_{3/2}^{4+}]O_{4}$  (M = Mg, Ni, and Mn) is determined by competition between  $J_{1,d}$  and  $J_{1,s}$ . Here, the distance between Mn<sup>4+</sup> ions ( $r_{\text{Mn-Mn}}$ ) at ca. 293 K is calculated as 2.882 Å for Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub>,<sup>(15,37,38)</sup> 2.888 Å for Li[Mg<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub>,<sup>(36)</sup> 2.887 Å for Li<sub>1/2</sub>Zn<sub>1/2</sub>[Li<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub>,<sup>(75)</sup> 2.820 Å for Li<sub>0</sub>[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub>,<sup>(15,37)</sup> and 2.833 Å for  $\lambda$ -MnO<sub>2</sub>.<sup>(37,40,42)</sup> Therefore, it is likely that  $J_{1,s}$  is dominant for Li[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub> and Li[Mg<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub>, while  $J_{1,d}$  is dominant for Li<sub>0</sub>[Ni<sub>1/2</sub>Mn<sub>3/2</sub>]O<sub>4</sub> and  $\lambda$ -MnO<sub>2</sub>. Such a variation from FM to AF ordering with  $a_c$  is also observed for a series of chromium spinels, ACr<sub>2</sub>X<sub>4</sub> (A= Mg, Zn, and Cd: X = O, S, and Se)<sup>(77)</sup>, in which the Cr<sup>3+</sup> ions are in the S = 3/2 ( $t_{2g}^3 e_g^0$ ) state; CdCr<sub>2</sub>S<sub>4</sub> with  $r_{\text{Cr-Cr}} = 3.61$  Å is FM ( $T_{\text{C}} = 85$  K), and CdCr<sub>2</sub>O<sub>4</sub> with  $r_{\text{Cr-Cr}} = 3.03$  Å is AF ( $T_{\text{N}} = 9$  K).

# **3.4** Comparison between Electrochemical and Chemical Delithiated Reactions<sup>(40-42)</sup>

Although a non-aqueous electrolyte is used in current LIBs, it is widely recognized that acid treatment with an aqueous solution produces a fully delithiated phase. Hunter reported<sup>(78)</sup> that fully delithiated Li<sub>x</sub>Mn<sub>2</sub>O<sub>4</sub> ( $\lambda$ -MnO<sub>2</sub>) is prepared by immersion of LiMn<sub>2</sub>O<sub>4</sub> in an acid solution according to the following disproportionation reaction:

$$4\text{LiMn}^{3+} \text{Mn}^{4+} \text{O}_4(\text{sol.}) + 8\text{H}^+ \rightarrow 6\lambda - \text{Mn}^{4+} \text{O}_2(\text{sol.}) + 2\text{Mn}^{2+}(\text{liq.}) + 4\text{Li}^+ + 4\text{H}_2\text{O} \cdots \cdots \cdots \cdots \cdots \cdots (11)$$

This is because acid treatment in a solution with sufficient  $H^+$  corresponds to the voltage 1.23 V vs. standard hydrogen electrode (SHE) and is eventually equivalent to the electrochemical charging up to ca. 4.2 V vs. Li<sup>+</sup>/Li.<sup>(79)</sup> However, the chemical delithiation process should be different from the electrochemical delithiation process, because the disproportionation reaction described in Eq. (11) always involves dissolution from a particle, and consequently, the solid-liquid interface is renewed during the reaction. Thus, we have investigated the structural and magnetic natures of both electrochemically (EC-) and chemically (C-) prepared Li<sub>x</sub>Mn<sub>2</sub>O<sub>4</sub> and Li<sub>x</sub>NiO<sub>2</sub> samples by XRD,  $\chi$ ,  $\mu$ SR, and thermal analyses.

**Figure 15** shows the *T* dependence of  $\chi^{-1}$  for the Li<sub>*x*</sub>Mn<sub>2</sub>O<sub>4</sub> and Li<sub>*x*</sub>NiO<sub>2</sub> samples prepared by both ECand C-reactions.  $\chi$  was measured in FC mode with H = 10 kOe. The  $\chi^{-1}(T)$  curve for C-Li<sub>0.07</sub>Mn<sub>2</sub>O<sub>4</sub> is almost the same as that for EC-Li<sub>0.03</sub>Mn<sub>2</sub>O<sub>4</sub>. As Tdecreases from 350 K, the  $\chi^{-1}(T)$  curves for all samples exhibit Curie-Weiss paramagnetic behavior down to ca. 200 K, except for the cusp at  $T_{\rm JT}$  (= 285 K). Using Eq. (9) in the T range between 200 and 350 K, values of  $\mu_{eff}$  and  $\Theta_p$  were obtained for the Li<sub>x</sub>Mn<sub>2</sub>O<sub>4</sub> samples and are given in **Table 1**. Here,  $\mu_{eff}^{pre}$  is calculated under the assumption that Mn<sup>3+</sup> ions are in the high-spin state with  $S = 2 (t_{2g}^3 e_g^1)$ , Mn<sup>4+</sup> ions with  $S = 3/2 (t_{2g}^3 e_g^0)$ , and g = 2.  $\mu_{eff}$  obtained for both the EC-Li<sub>0.03</sub>Mn<sub>2</sub>O<sub>4</sub> and C-Li<sub>0.07</sub>Mn<sub>2</sub>O<sub>4</sub> samples are very close to  $\mu_{eff}^{pre}$ , so that  $\mu_{eff}$  for both samples are well explained by the Mn valence estimated from the Li/Mn ratio. Figure 15(b) shows that the  $\chi^{-1}(T)$  curve for C-Li<sub>0.01</sub>NiO<sub>2</sub> is very different from that for EC-Li<sub>0.05</sub>NiO<sub>2</sub>; the magnitude of  $\chi^{-1}$  for C-Li<sub>0.01</sub>NiO<sub>2</sub> is smaller than that for EC- $Li_{0.05}NiO_2$  in the entire T range measured. Furthermore, as given in Table 1,  $\mu_{eff}$  for C-Li<sub>0.01</sub>NiO<sub>2</sub> (= 1.43  $\mu_B$ ) is approximately twice that for EC-Li<sub>0.05</sub>NiO<sub>2</sub> (= 0.71 $\mu_B).$  Here,  $\mu_{eff}$  for LiNiO\_2 is larger by 0.3  $\mu_B$  than  $\mu_{eff}^{\text{pre}},$ which is calculated by the assumption that Ni<sup>3+</sup> and Ni<sup>4+</sup> ions are in the low-spin state with  $S = 1/2 (t_{2g}^6 e_g^1)$ and S = 0 ( $t_{2g}^6 e_g^0$ ), respectively, and g = 2. The difference



**Fig. 15** Temperature dependence of  $\chi^{-1}$  for (a) Li<sub>x</sub>Mn<sub>2</sub>O<sub>4</sub> and (b) Li<sub>x</sub>NiO<sub>2</sub> samples measured in FC mode with H = 10 kOe. The EC-Li<sub>0.03</sub>Mn<sub>2</sub>O<sub>4</sub> and EC-Li<sub>0.05</sub>NiO<sub>2</sub> samples were prepared by electrochemical (EC-) reaction, while the C-Li<sub>0.07</sub>Mn<sub>2</sub>O<sub>4</sub> and C-Li<sub>0.01</sub>NiO<sub>2</sub> samples were prepared by chemical (C-) reaction.  $T_{\rm JT}$  represents the Jahn-Teller (JT) transition temperature.

between  $\mu_{eff}$  and  $\mu_{eff}^{pre}$  is probably due to an enhancement of the g-factor caused by local JT distortion of the NiO<sub>6</sub>-octahedra.<sup>(80)</sup> Thus, the average valence for C-Li<sub>0.01</sub>NiO<sub>2</sub> is not simply determined by the Li/Ni ratio, even if we consider enhancement of the g-factor and/or analytical error in the Li/Ni ratio of the ICP-AES analysis data ( $\delta x = 0.01$ ).<sup>(40)</sup>

According to the structural analyses of Li<sub>r</sub>Mn<sub>2</sub>O<sub>4</sub> and  $Li_xNiO_2$ , the oxygen stacking sequence for  $Li_xMn_2O_4$ is maintained in the *ccp* structure down to  $x \approx 0.^{(4\overline{2},78)}$ However, those for both EC-Li<sub>x</sub>NiO<sub>2</sub><sup>(65)</sup> and C-Li<sub>x</sub>NiO<sub>2</sub><sup>(66)</sup> are partially converted from the *ccp* structure to the *hcp* structure below  $x \approx 0.1$ . Note that proton insertion materials such as NiOOH and CoOOH for Ni-MH batteries have the hcp structure with an ABAB oxygen stacking sequence, while lithium insertion materials such as LiNiO<sub>2</sub> (NiOOLi) and LiCoO<sub>2</sub> (CoOOLi) for LIBs have the *ccp* structure with an ABCABC oxygen stacking sequence. Thus, the structural variation from the *ccp* to *hcp* structure in  $\text{Li}_x \text{NiO}_2$  with  $x \leq 0.1$ naturally induces proton insertion into the material.

**Figure 16**(a) shows the *T* dependence of  $N_{\text{ATF}}$  for the EC-Li<sub>0.10</sub>NiO<sub>2</sub> and C-Li<sub>0.01</sub>NiO<sub>2</sub> samples obtained by wTF-µSR measurements. For the EC-Li<sub>0.10</sub>NiO<sub>2</sub> sample, as T decreases from 50 K,  $N_{\text{ATF}}$  is ca. 1 down to ca. 20 K, then slightly decreases by ca. 0.1 with further decrease in T, which is consistent with the majority non-magnetic 4+ state of the Ni ions with

Table 1 Effective magnetic moment ( $\mu_{eff}$ ) and Curie-Weiss temperature ( $\Theta_p$ ) for Li<sub>x</sub>Mn<sub>2</sub>O<sub>4</sub> and Li<sub>x</sub>NiO<sub>2</sub>.

в <sup>с</sup>

<sup>a</sup> Li<sub>x</sub>Mn<sub>2</sub>O<sub>4</sub> and Li<sub>x</sub>NiO<sub>2</sub> samples were prepared by both electrochemical (EC-) and chemical (C-) reactions.  $^b$  The values of  $\mu_{eff}$  and  $\Theta_p$  were obtained by fitting the  $\chi$ 

vs. T curve in the T range between 200 and 350 K.

 $^{c}\ \mu_{eff}^{pre}$  is the predicted effective magnetic moment for  $\text{Li}_x \text{Mn}_2 \text{O}_4$  and  $\text{Li}_x \text{NiO}_2$  calculated assuming that  $\text{Mn}^{3+}$  ions are in the high-spin state with  $S = 2 (t_{2g}^3 e_g^1)$ ,  $\text{Mn}^{4+}$  ions with  $S = 3/2 (t_{2g}^3 e_g^0)$ , Ni<sup>3+</sup> ions with  $S = 1/2 (t_{2g}^6 e_g^0)$ , Ni<sup>4+</sup> ions with S = 0  $(t_{2g}^6 e_g^0)$ , and g = 2.

S = 0  $(t_{2g}^6 e_g^0)$ . For the C-Li<sub>0.01</sub>NiO<sub>2</sub> sample, as T decreases from 50 K, the  $N_{\text{ATF}}(T)$  curve shows two step-like drops at ca. 15 K and below 10 K, although  $N_{\text{ATF}} = 0.32$  even at 1.8 K. This indicates that (i) magnetic Ni ions are still present in the sample, as expected from the value of  $\mu_{eff}$ , (ii) there are at least three different magnetic phases denoted as M1, M2, and M3 in the sample, and (iii) approximately 1/3 of the sample is still PM even at 1.8 K. Figure 16(b) shows the ZF- $\mu$ SR spectra for the EC-Li<sub>0.10</sub>NiO<sub>2</sub> and C-Li<sub>0.01</sub>NiO<sub>2</sub> samples at 15 at 12.5 K, respectively. Note that both samples are in the PM state, as shown in Fig. 16(a). In the PM state, muon-spins should be depolarized by the randomly oriented nuclear magnetism, not by the electronic magnetism. Therefore, the ZF-µSR spectrum is fitted by a dynamic  $KT^{(47)}$  function,  $G^{DGKT}(t, \Delta, v)$ :

$$A_0 P_{\rm ZF}(t) = A_{\rm KT} G^{\rm DGKT}(\Delta, v, t) + A_{\rm fast} \exp(-\lambda_{\rm fast} t),$$
  
....(12)

where  $A_{\rm KT}$  and  $A_{\rm fast}$  are the asymmetries of the KT (PM) phase and residual magnetic phase, respectively, and  $\lambda_{\rm fast}$  is the relaxation rate of the magnetic phase.



**Fig. 16** (a) Temperature dependence of the normalized wTF-asymmetries ( $N_{ATF}$ ) for the EC-Li<sub>0.10</sub>NiO<sub>2</sub> and C-Li<sub>0.01</sub>NiO<sub>2</sub> samples. (b) ZF- $\mu$ SR spectra for the EC-Li<sub>0.10</sub>NiO<sub>2</sub> sample at 15 K and for the C-Li<sub>0.01</sub>NiO<sub>2</sub> sample at 12.5 K. The solid lines in (b) indicate the fitting results from Eq. (12).

The ZF- $\mu$ SR spectrum for EC-Li<sub>0.10</sub>NiO<sub>2</sub> shows a slow relaxation, which indicates that muon-spins are mainly depolarized by the nuclear magnetic moment of Li. In contrast, the ZF-µSR spectrum for C-Li<sub>0.01</sub>NiO<sub>2</sub> shows a large relaxation.  $\Delta$ , which corresponds to the internal magnetic field, is calculated as  $0.075(2) \ \mu s^{-1}$  at 12.5 K for the EC-Li<sub>0.10</sub>NiO<sub>2</sub> sample, while it is calculated as  $0.355(3) \ \mu s^{-1}$  at 15 K for the C-Li<sub>0.01</sub>NiO<sub>2</sub> sample. Note that the C-Li<sub>0.01</sub>NiO<sub>2</sub> sample is almost fully delithiated. This indicates that there is another origin for the large relaxation observed only for the C-Li<sub>0.01</sub>NiO<sub>2</sub> sample. The nuclear magnetic moment caused by both the O and Ni nuclei is negligibly small; therefore, the large relaxation for the C-Li<sub>0.01</sub>NiO<sub>2</sub> sample is most likely due to the nuclear magnetic moment of the <sup>1</sup>H nucleus. Thus, the  $\mu$ SR result suggests the presence of H<sup>+</sup> ions in the C-Li<sub>0.01</sub>NiO<sub>2</sub> sample, although a proton-free model was previously proposed for C-Li<sub>x</sub>NiO<sub>2</sub>.<sup>(66)</sup>

In order to confirm the absence/presence of oxygen deficiency and H<sup>+</sup> ions, thermogravimetry (TG) and pyrolysis gas chromatography/mass spectroscopy (Py-GC/MS) analyses were conducted. **Figure 17**(a) shows the TG curve for the C-Li<sub>0.01</sub>NiO<sub>2</sub> sample. As *T* increases from ambient *T*, the TG curve decreases slightly above ca. 380 K, then decreases significantly around 473 K, and finally maintains an almost constant value until 873 K. After the acid reaction, the C-Li<sub>0.01</sub>NiO<sub>2</sub> sample was dried at only 40°C in an



Fig. 17 (a) Thermogravimetric curve and (b) Py-GC/MS spectrum for the  $C-Li_{0.01}NiO_2$  sample.

air-oven to avoid decomposition of the sample. Thus, the decrease around 380 K is most likely due to absorbed and/or adsorbed water. The weight loss at 1273 K (= m(1273 K) - m(300 K)) is ca. 17.7%, which is in good agreement with the expected change (= 17.6%) from the following oxygen evolution reaction:

This suggests the absence of oxygen deficiencies in the C-Li<sub>0.01</sub>NiO<sub>2</sub> sample, as reported previously.<sup>(66)</sup> Note that it is difficult to distinguish the absence/presence of H<sup>+</sup> ions in the C-Li<sub>0.01</sub>NiO<sub>2</sub> sample from the TG curve, because the weight loss is calculated as ca. 81.5% for the HNiO<sub>2</sub> (NiOOH) composition.

In contrast, two spectral features, which are identified as  $O^{2+}$  (mass/charge = 32) and  $H_2O^+$ (mass/charge = 18) ions, are clearly observed in the Py-GC/MS spectrum measured at 522 K (see Fig. 17(b)). This unambiguously demonstrates the presence of  $H^+$ ions in the C-Li<sub>0.01</sub>NiO<sub>2</sub> sample, which is consistent with the  $\chi$  and  $\mu$ SR measurement results. Here, it should be noted that the trend for the  $H_2O^+$  spectrum is very similar to that for the  $O^{2+}$  spectrum; both spectra show two peaks at ca. 490 and 535 K. This indicates that structurally bonded and/or intercalated water is present in the C-Li<sub>0.01</sub>NiO<sub>2</sub> crystalline lattice. The TG curve for the Ni(OH)<sub>2</sub> compound showed two weight loss regions in the T ranges of 323-363 K and 453-723 K, which are attributed to dehydration reactions of absorbed/adsorbed water and structurally bonded/intercalated water, respectively. Therefore, the decomposition reaction for the C-Li<sub>0.01</sub>NiO<sub>2</sub> sample is represented by:

 $H_{x}Li_{0.01}NiO_{2} \cdot yH_{2}O \rightarrow H_{x}Li_{0.01}NiO_{2} + yH_{2}O_{2}$ (380-470 K) · · · (14)  $H_{x}Li_{0.01}NiO_{2} \rightarrow Li_{0.01}NiO + x/2H_{2}O + (1 - x/4)O_{2}$ (470-870 K) · · · (15)

The total amount of  $H^+$  ions in the C-Li<sub>0.01</sub>NiO<sub>2</sub> sample is evaluated as ca. 0.5, i.e.  $H_{-0.5}Li_{0.01}NiO_2$ , from the linear relationship between  $\mu_{eff}$  and x in the EC-Li<sub>x</sub>NiO<sub>2</sub> sample. Thus, the vacant tetrahedral or octahedral sites in C-Li<sub>0.01</sub>NiO<sub>2</sub> are partially occupied by  $H^+$  ions. In this calculation, it was assumed that both Ni<sup>3+</sup> and Ni<sup>4+</sup> ions are in the low-spin state, because Ni ions occupy the octahedral sites in both the *ccp* and *hcp* structures. The results of wTF-µSR measurements

also support this assumption; Fig. 16(a) indicates that three different magnetic phases of M1, M2, and M3 are present according to the T dependence of  $N_{\text{ATF}}$ , which indicates the inhomogeneity of the sample. The volume fraction of the M1, M2, and M3 phases is approximately 40, 30, and 30%, respectively.  $T_{\rm m}$  of the M1 (M2) phase is almost the same as that for the  $EC-Li_{0.60}NiO_2$  ( $EC-Li_{0.50}NiO_2$ ) sample;<sup>(32,33,41)</sup> therefore, the average valence of Ni ions  $(V_{\text{Ni}}^{\text{ave}})$  for the C-Li<sub>0.01</sub>NiO<sub>2</sub> sample is estimated as ca. 3.6 (=  $4 - 0.6 \times 0.4 - 0.5 \times$ 0.3). This is consistent with the  $\chi$  measurement results  $(V_{\rm Ni}^{\rm ave} \sim 3.5)$ . We emphasize that the detection of H<sup>+</sup> ions in LIB materials is significantly important for improvement of the cycling and storage performance at elevated temperatures above 55°C. This is because electrochemical charging at high voltages above 4.2 V sometimes generates H<sup>+</sup> ions, which results from the decomposition of non-aqueous electrolytes, such as the case for  $Li_2MnO_3.^{(81)}\chi$  and  $\mu SR$  are therefore powerful techniques to investigate such phenomena.

#### 4. Conclusion

Magnetic susceptibility ( $\chi$ ) analysis and muon-spin rotation/relaxation ( $\mu$ SR) spectroscopy were used to elucidate the electrochemical reaction scheme of lithium insertion materials through their macro- and microscopic magnetic nature. A trial-and-error methodology is usually employed on an empirical basis to design advanced lithium insertion materials. However, the author believes that an in-depth understanding of the properties of materials can lead to the development of new functions or materials, because "Buds of science" come from growing "Why" in mind. Magnetic measurements are one such powerful tool to develop a deeper understanding of material properties.

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